

# Weak-Consistency Specification via Visibility Relaxation

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# Motivation

# Concurrent Objects

## High-level abstractions

e.g. numeric & collection ADTs

## Low-level performance

e.g. lock-free shared-memory access

## Available on modern platforms

e.g. dozens in JDK

```
/**  
 * a concurrent collection is thread-  
 * safe, but not governed by a single  
 * exclusion lock.  
 */  
package java.util.concurrent;
```

```
// we've considered these objects  
class ConcurrentHashMap { ... }  
class ConcurrentSkipListMap { ... }  
class ConcurrentSkipListSet { ... }  
class ConcurrentLinkedQueue { ... }  
class LinkedTransferQueue { ... }  
class LinkedBlockingQueue { ... }  
class ConcurrentLinkedDeque { ... }
```

```
// and there are several more
```

# Weak Consistency

## Performance optimization

avoid synchronization bottlenecks

weaken guarantees

## Out in the wild

e.g. collections in JDK

## Undermines reasoning

“Weakly consistent” is imprecise

```
package java.util.concurrent;
class ConcurrentSkipListSet { ... }

/**
 * Iterators and spliterators are
 * weakly consistent...
 *
 * They are guaranteed to traverse
 * elements as they existed upon
 * construction exactly once and may
 * (but are not guaranteed to) reflect
 * any modification subsequent to
 * construction.
 */
```

# E.g. The Size Method

```
/**  
 * ... the size method is not a  
 * constant-time operation...  
 * determining the current number of  
 * elements requires a traversal of  
 * the elements ... may report  
 * inaccurate results if ... modified  
 * during traversal.  
 */  
class ConcurrentSkipListMap { ... }
```

## Requirements?

allow  $n = 0$

forbid  $n = -1, 42, 100, \dots$

## Generic methodologies?

not tied to sets nor sizes

reuse existing functional spec

```
new Thread() -> {  
    s.add(1);  
    s.remove(2);  
}.start();  
  
new Thread() -> {  
    s.add(2);  
    var n = s.size();  
}.start();
```

## ADT-admitted linearizations

```
add(1); remove(2); add(2); size() => 2  
add(1); add(2); remove(2); size() => 1  
add(1); add(2); size() => 2; remove(2)  
add(2); add(1); remove(2); size() => 1  
add(2); size() => 1; add(1); remove(2)
```

# Visibility Relaxation

## Axiomatic framework

Linearization + visibilities

Burckhardt et al.

## Which criterion?

causal consistency  
*doesn't allow  $n = 0$*

eventual consistency  
*doesn't constrain  $n$  at all*

## How to mix?

add & remove remain atomic

## Linearization

`add(1); add(2); remove(2); size() => n`

visibility of size			
add(1)	add(2)	remove(2)	$n$
		✓	0
	✓		0
✓			1
✓	✓	✓	0
✓		✓	1
✓	✓	✓	2
✓	✓	✓	1

# Contributions

## Visibility Relaxation

an annotation language

## Sequential happens-before consistency (SHBC)

effective consistency validation

## Empirical study

derive JDK specifications

```
interface WeakSizeSet<E> {  
    // complete visibility  
    public boolean add(E elem);  
  
    // complete visibility  
    public boolean remove(E elem);  
  
    // monotonic visibility  
    public monotonic int size();  
}
```

# **Visibility Relaxation**

# Programs & Behaviors

## Program Order (PO)

per-thread invocation order

## Happens-Before (HB)

PO with synchronization

## Outcome

invocations' return values

## Behavior

HB with outcome

## Implementation

maps programs to behaviors

**Program**  
{ add(1); remove(2) } || { add(2); **size()** }

**Implementation**  
ConcurrentSkipListSet

## Behaviors/Outcomes

[ false, true, false, **0** ]  
[ false, true, false, **1** ]  
...

# Linearizations

## Linearization Order

total order over invocations

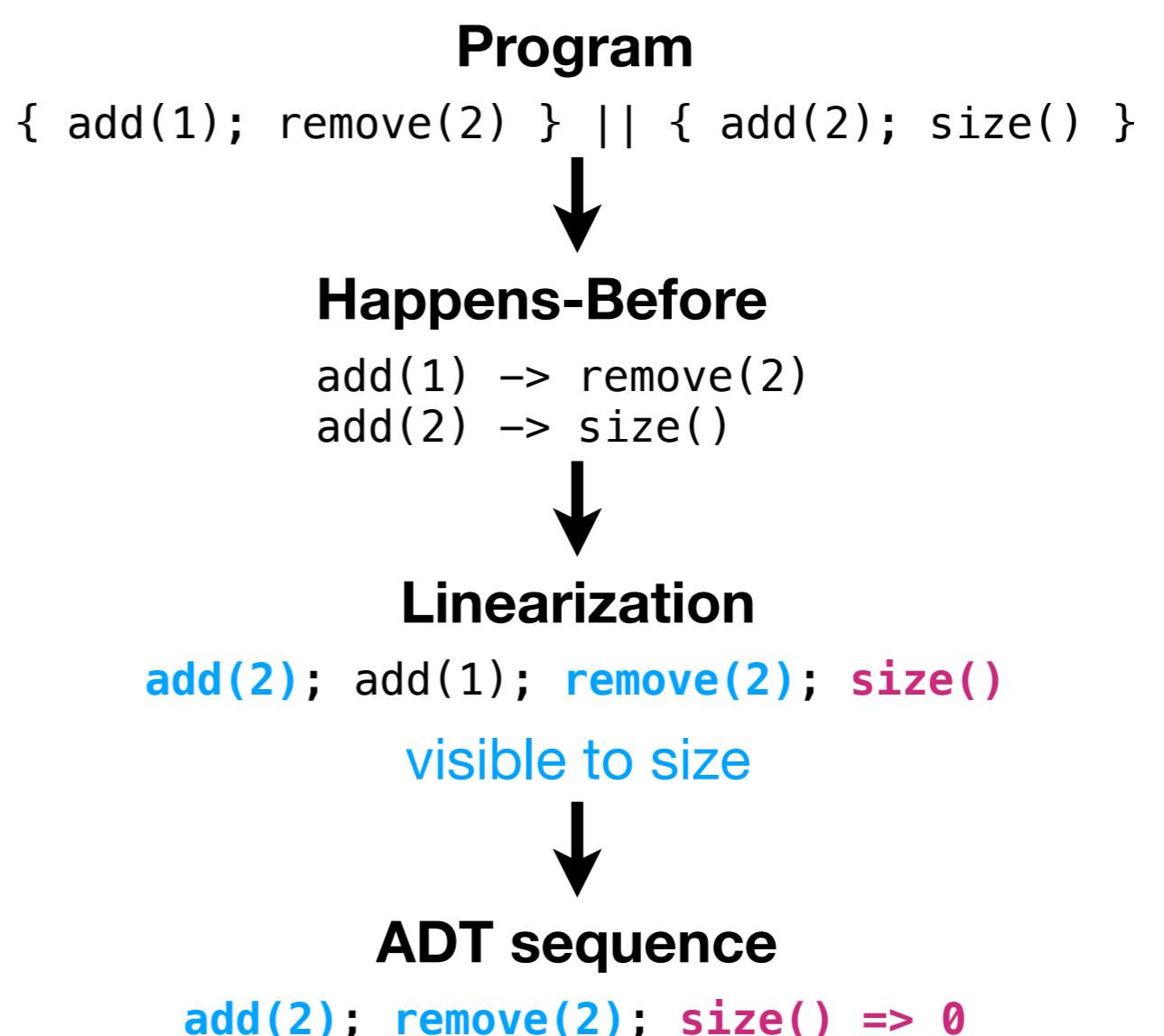
includes happens-before

## Visibility Relation

subsequence of linearized-before

## ADT Consistency

subsequence admits return value



# Predicates & Specifications

## Visibility Predicates

lower bounds on visibility

## Visibility Specification

one predicate per method

## Consistency

only consider linearizations satisfying  
per-method predicates

### weak

no constraints

### basic

must see happened-before

### monotonic

also must see those seen by happens-before

### peer

also must see those which happened before seen

### causal

also visibility is transitive

### complete

must see all linearized before

# E.g. The Size Method

## Consistent w/ monotonic

size sees add(2)

and all seen by add(2)

i.e. *none*

## Inconsistent w/ peer

size sees remove(2)

not HB-predecessor add(1)

## Program

```
{ add(1); remove(2) } || { add(2); size() }
```



## Happens-Before

add(1) -> remove(2)

add(2) -> size()



## Linearization

```
add(2); add(1); remove(2); size()
```

visible to size



## ADT sequence

```
add(2); remove(2); size() => 0
```

# Assertion-Based Validation

**Compute expected behaviors**

for a given test program

**Record observed behavior**

return values & happens-before

**Assert the inclusion**

e.g. via hashing

```
function expected({ po, hbs }, Impl, Spec) {  
    for (let hb of hbs) {  
        for (let { lin, vis } of hb.lins()) {  
            if (!Spec.isSatisfied(lin, vis, hb))  
                continue;  
            let ret = {};  
            for (let i of lin) {  
                let seq = vis(i);  
                let res = Impl.execute(seq);  
                ret[i] = res[res.length - 1];  
            }  
            yield { hb, ret };  
        }  
    }  
}
```

# **Sequential Happens-Before Consistency**

# vs. Linearizability

## Real-Time (RT) Order

return action precedes call

platform agnostic

## Happens-Before (HB) Order

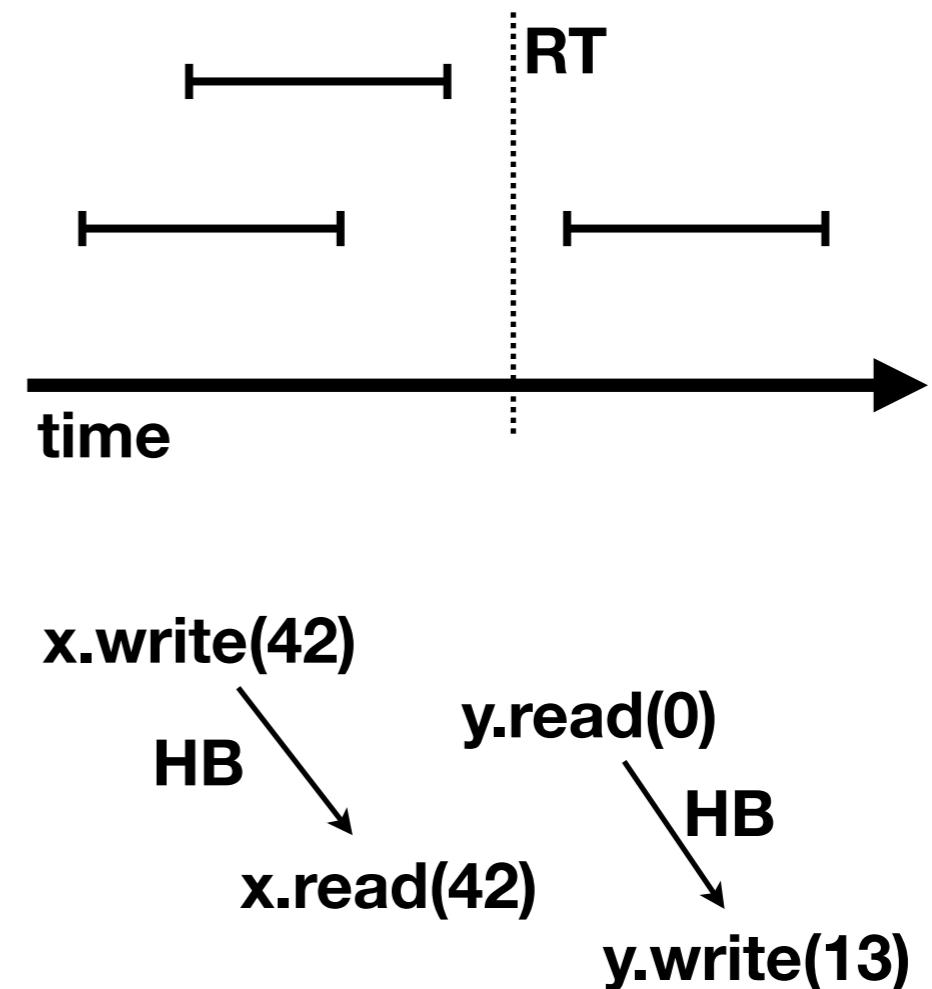
platform dependent

e.g. Java volatile variables, locks

## Sequential HB Consistency

linearizations of HB, not RT

extends SC from PO to HB



# Real-Time

## Runtime monitoring?

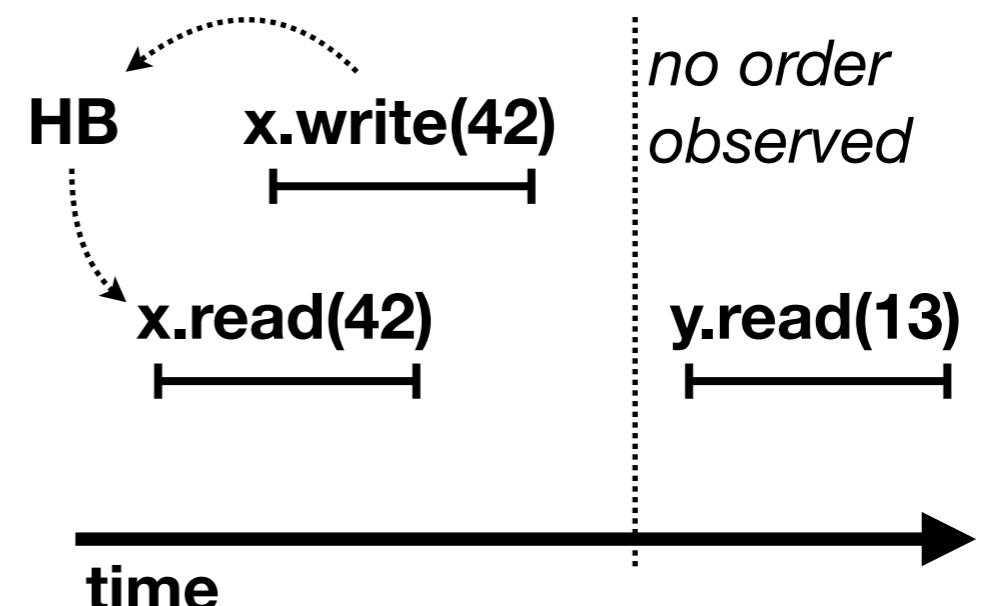
platform specs eschew guarantees  
recording mechanisms interfere

## Sound linearizability?

impossible w/o platform guarantees!

## Leverage happens-before?

LIN becomes SHBC



# Platform Properties

## Real-Time Soundness (RTS)

happens-before implies real-time

## Real-Time Consistency (RTC)

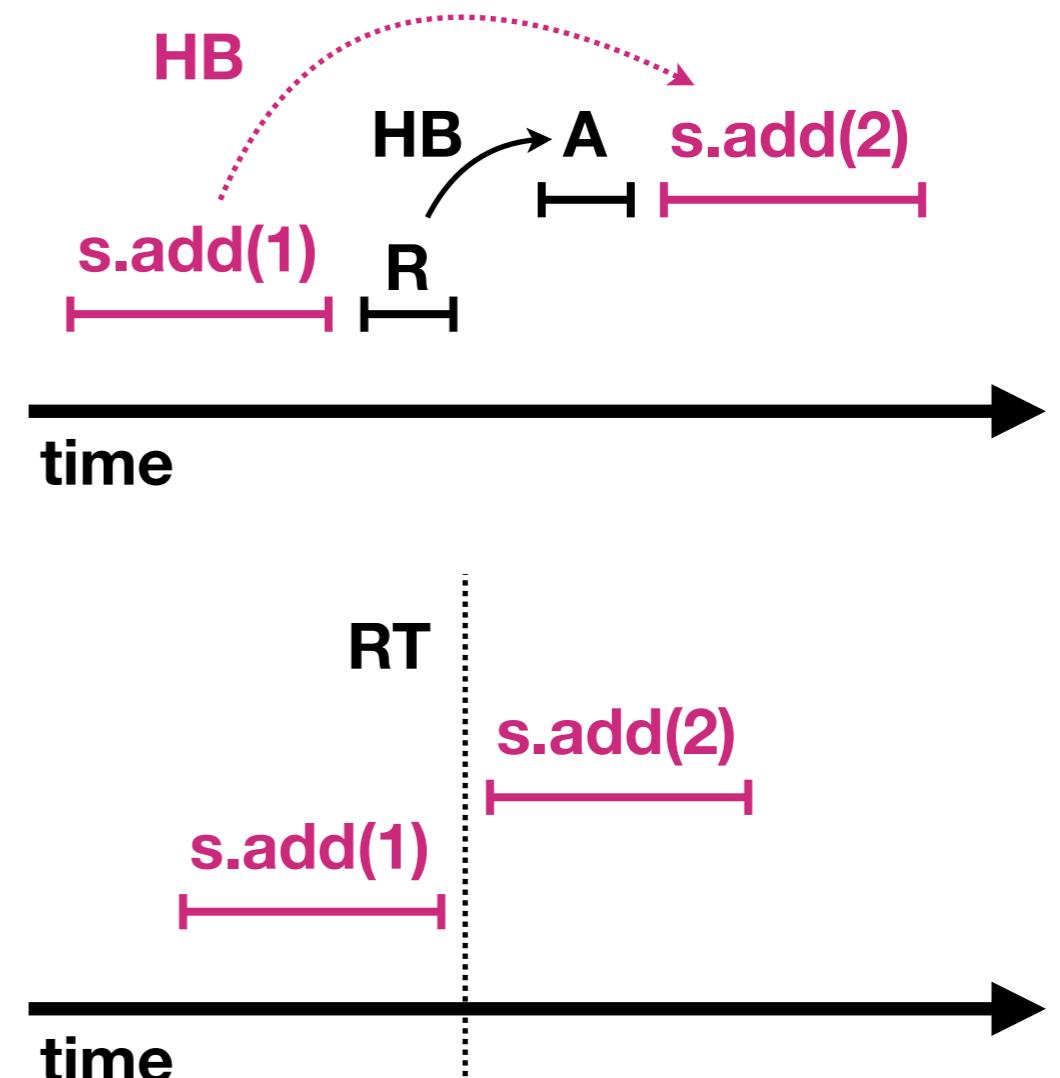
real-time implies happens-before\*

(without interference)

## Real-Time Limit Consistency

every admitted real-time order is captured\* by a happens-before order

\*given sufficient instrumentation



# Real-Time Instrumentation

## Memory-Based

requires instruction barriers

requires atomic read-call & ret-write

requires location independence (PSO)

## Clock-Based

requires high-precision

requires negligible latency

requires atomic read-call & ret-read

```
// invocation 1
boolean[] before1 = {
    done[I3],
    done[I4]
};
s.add(1);
done[I1] = true;

// invocation 2
boolean[] before2 = {
    done[I3],
    done[I4]
};
s.add(2);
done[I2] = true;

// reconstruct order
boolean[][] before = {
    before1,
    before2
};
```

# **Equivalences**

**LIN implies SHBC**

for RTS platforms

**SHBC implies LIN**

per execution, on RTC platforms

**SHBC implies LIN**

per object, on RTCL platforms

# **Empirical Study**

# Hypotheses

## **Atomicity**

JDK methods not generally atomic

## **Specification**

with visibility annotations

## **Validation**

SHBC uncovers violations

# Empirical Setup

## 7 JDK collections

Maps, Sets, Queues, Deques

## Random Test Generation

2 threads, 3–6 invocations, 1–2 values

100K programs per object

## Stress Testing

1 second per test program

## Simplification

without synchronization

### ConcurrentHashMap: size

{ put(1,0); put(1,1); size() } || { remove(1) }

outcome	atomic?	frequency
null, 0, 0, 1	✓	949
null, 0, 1, 1	✓	746,263
null, 0, 1, null	✓	2,614,780
null, null, 1, 0	✓	14,833
null, null, 2, 0	✗	35

# JDK Atomicity

## 50+ non-atomic methods

roughly 40% of those tested

### Some predictable

docs mention weak consistency

e.g. `size`, `iterator`, `elements`, ...

### Others unexpected

breaks internal invariants

e.g. `clear`

weak-memory behaviors

e.g. `final` keyword missing from `peekLast`, ...

program / method	ConcurrentHashMap	outcome	frequency
{put(0,0); put(1,1); put(1,1)}    {p	N,N,N,N,()	1 / 2,845,260	
{put(0,0);remove(1)}    {put(1,0);co	N,0,N,F	6 / 1,508,770	
{get(1);containsValue(1)}    {put(1,	1,F,N,N,1	1 / 3,993,110	
{put(0,1);put(1,0)}    {elements()}	N,N,[0]	3 / 1,665,650	
{put(0,1);put(1,0)}    {entrySet()}	N,N,[1=0]	23 / 2,688,890	
{ put(1,1) }    { put(1,2); isEmpty()	N,1,T	57 / 4,136,690	
{put(0,1);put(1,1)}    {keySet()}	N,N,[1]	18 / 5,048,060	
{keys()}    {put(0,1);put(1,1)}	[1],N,N	13 / 1,721,300	
{put(1,0); put(1,1); mappingCount(	N,N,2,0	52 / 2,231,190	
{put(1,0); put(1,1); size()}    {remo	N,N,2,0	57 / 2,659,700	
{put(0,1);put(1,1)}    {toString()}	N,N,1=1	120 / 3,948,560	
{put(0,1);put(1,0)}    {values()}	N,N,[0]	99 / 2,836,280	

# JDK Specification

**84 complete**

mostly single-element operations

**29 monotonic**

meaning of “weakly consistent?”

**3 weak**

isEmpty, toArray, toString

**18 inconsistent**

most indicate bugs

few are intended

**e.g. ConcurrentHashMap**

**complete**

put, get, remove, containsKey, replace,  
putIfAbsent

**monotonic**

contains, containsValue, keys, values,  
elements, entrySet, keySet, toString

**weak**

isEmpty

**inconsistent**

clear, size, mappingCount

# JDK Validation

**SHBC is effective**

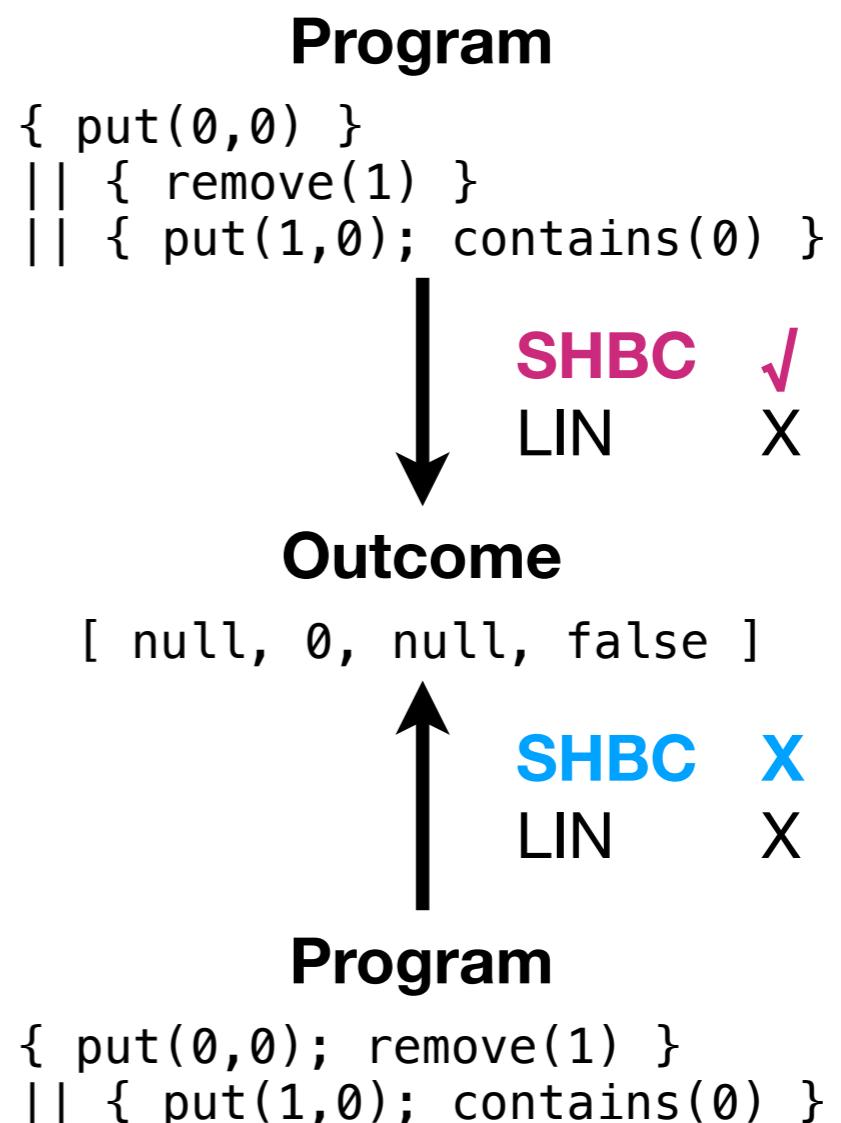
identifies violations w/o real-time

**SHBC is efficient**

millions of executions per second

**Randomness useful**

e.g. unexpected argument combos



# Conclusion

## **Visibility relaxation**

generic yet precise semantics

## **Sequential happens-before consistency**

efficient validation

integration with modern platforms

## **Empirical study**

effective specification and validation